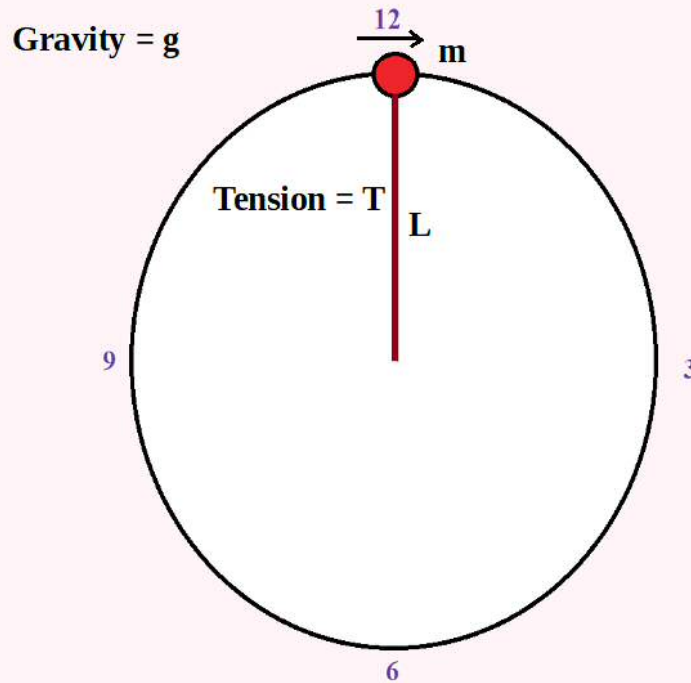


## Rotation in a Vertical Plane



A ball of mass  $m$  is rotating clockwise in a vertical circle of radius  $L$ . The tension in the string when the ball is passing the 12 o'clock position is  $T$ . What should be the tension in the string at the 3 o'clock position? For gravity use  $g$ . Write your answer in terms of  $m$ ,  $L$ ,  $g$ , and  $T$ .

### SOLUTION:

First we do a balance of forces at 12 o'clock:

Centrifugal force = Tension + Weight

$$m \cdot v^2 / L = T + m \cdot g$$

$$m \cdot v^2 = L(T + m \cdot g)$$

KE at 12 o'clock is:  $KE = (1/2) \cdot m \cdot v^2$

$$KE = (1/2) \cdot L(T + m \cdot g)$$

A balance of energy between 12 o'clock and 3 o'clock gives:

$$KE_{12} + PE_{12} = KE_3$$

$$(1/2) \cdot L(T + m \cdot g) + m \cdot g \cdot L = (1/2) \cdot m \cdot v_3^2$$

$$\text{Thus: } L(T + m \cdot g) + 2 \cdot m \cdot g \cdot L = m \cdot v_3^2$$

At 3 o'clock the tension  $T_3$  in the string is equal to the centrifugal force:

$$T_3 = m \cdot v_3^2 / L$$

$$T_3 = [L(T + m \cdot g) + 2 \cdot m \cdot g \cdot L] / L =$$

$$T_3 = T + 3 \cdot m \cdot g$$